

1.

The graph above shows the number of hours 5 students spend listening to music each day.

a) Who listens to the greatest number of hours?

Ling Yee

Answer: ..... [1]

b) How many more hours did Samuel listen to music than Rajesh?

$$16 - 12 = 4 \text{ hours}$$

Answer: ..... [1]

2

a) Express 420 as a product of its prime numbers.

$$420 = 2^2 \times 3 \times 5 \times 7$$

Answer: ..... [1]

b) Write down the smallest positive integer,  $k$ , such that  $420k$  is a perfect cube.

$$\begin{aligned}
 2^2 \times 3 \times 5 \times 7 &= 420 \\
 2^2 \times 2 \times 3 \times 3^2 \times 5 \times 5^2 \times 7 \times 7^2 &= 420k \\
 2^2 \times 3 \times 5 \times 7 \times 2 \times 3^2 \times 5^2 \times 7^2 &= 420 \times k \\
 \therefore k &= 2 \times 3^2 \times 5^2 \times 7^2 \\
 k &= 22050
 \end{aligned}$$

Answer: ..... [1]

3

a) What is the speed of a car if it takes 6 hours to travel 489 kilometres?

$$\begin{aligned} \text{speed} &= \frac{\text{distance}}{\text{time}} \\ &= \frac{489}{6} \\ &= 81.5 \text{ km/h} \end{aligned}$$

Answer: ..... [1]

b) What is the speed of the same car in m/s?

$$\begin{aligned} \text{speed} &= \frac{\text{distance}}{\text{time}} \\ &= \frac{489}{6} \\ &= \frac{489000}{6 \times 60 \times 60} \\ &= 22.6 \text{ m/s} \end{aligned}$$

Answer: ..... [1]

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4

a) Express 18% as a decimal.

$$\frac{18}{100} = 0.18$$

Answer: ..... [1]

b) Express 36 as a percentage of 50.

$$\begin{aligned} &\frac{36}{50} \% \\ &= \frac{36}{50} \times 100 \\ &= 72\% \end{aligned}$$

Answer: ..... [1]

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5.

Solve the inequality  $4x + 3 \geq 11$ .

$$4x + 3 \geq 11$$

$$4x \geq 11 - 3$$

$$4x \geq 8$$

$$x \geq \frac{8}{4}$$

$$x \geq 2$$

Answer: ..... [2]

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6.

Solve  $\frac{4}{3y} - 4 = 3$ .

$$\frac{4}{3y} - 4 = 3$$

$$\frac{4}{3y} = 7$$

$$3y = \frac{4}{7}$$

$$y = \frac{4}{7} \div 3$$

$$y = \frac{4}{21}$$

Answer: ..... [2]

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7.

Make  $m$  to be the subject of this formula.

$$\frac{2}{m - 3x} = y$$

$$2 = y(m - 3x)$$

$$2 = ym - 3xy$$

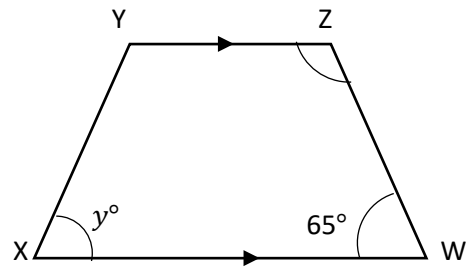
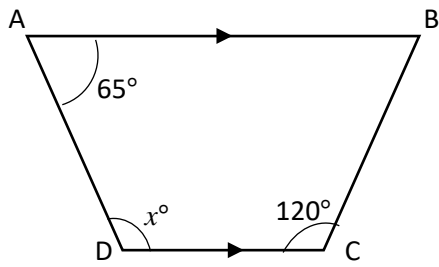
$$2 + 3xy = ym$$

$$\frac{2 + 3xy}{y} = m$$

$$m = \frac{3xy + 2}{y}$$

Answer: ..... [2]

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8.

These trapeziums ABCD and WXYZ are congruent to each other.

a) Find the value of  $\sphericalangle x$ .

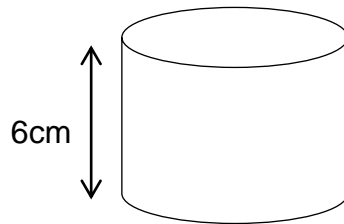
$$\sphericalangle x = 180 - 65 = 115^\circ (\text{supplementary angles})$$

Answer: ..... [1]

b) Find the value of  $\sphericalangle y$ .

$$\sphericalangle y = 360^\circ - 120 - 65 - 115 = 60^\circ$$

Answer: ..... [1]



9

Calculate the total surface area of the cylinder with radius and height of 6cm. [3]

$$\begin{aligned} \text{Total surface area of cylinder} &= 2\pi r^2 + \pi r h \\ &= 2\pi(36) + \pi(6)(6) \\ &= 72\pi + 36\pi \\ &= 108\pi \\ &= 320.442\text{cm}^2 \\ &= 320\text{cm}^2 \end{aligned}$$

10.

Solve these simultaneous equations.

$$3x + 5y - 11 = 0$$

$$6x + 7y - 16 = 0$$

$$3x + 5y = 11 \text{ ----- (x2) Eqn 1}$$

$$6x + 7y = 16 \text{ ----- (Eqn 2)}$$

$$6x + 10y = 22 \text{ ----- Eqn 1}$$

$$6x + 7y = 16 \text{ ----- Eqn 2}$$

$$\text{Eqn 1} - \text{Eqn 2}$$

$$3y = 6$$

$$y = 2$$

Subst.  $y = 2$  into Eqn 1

$$3x + 5(2) = 11$$

$$3x = 1$$

$$x = 1/3$$

$$(1/3, 2)$$

Answer:  $x = \dots\dots\dots$

$y = \dots\dots\dots$  [2]

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- a) Write as a single fraction in its simplest form  $\frac{3}{x-2} + \frac{2}{x+2}$ .

$$\begin{aligned} & \frac{3}{x-2} + \frac{2}{x+2} \\ &= \frac{3(x+2) + 2(x-2)}{(x-2)(x+2)} \\ &= \frac{3x+6+2x-4}{(x-2)(x+2)} \\ &= \frac{5x+2}{(x-2)(x+2)} \end{aligned}$$

Answer: ..... [2]

- b) Simplify  $\frac{2xy+4y}{2xy+6y}$ .

$$\begin{aligned} & \frac{2xy+4y}{2xy+6y} \\ &= \frac{2y(x+2)}{2y(x+3)} \\ &= \frac{x+2}{x+3} \end{aligned}$$

Answer: ..... [1]

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12.

Given that  $d$  is directly proportional to the square root of  $t$ .

a) Given that  $d = 8$  when  $t = 4$ , find  $d$  when  $t$  is 16.

$$\begin{aligned}d &= k\sqrt{t} \\8 &= k\sqrt{4} \\k &= 4\end{aligned}$$

$$\begin{aligned}d &= 4\sqrt{16} \\d &= 4(\sqrt{16}) \\d &= 16\end{aligned}$$

Answer: ..... [1]

b) Find the value of  $t$  when  $d = 20$

$$\begin{aligned}d &= 4\sqrt{t} \\20 &= 4\sqrt{t} \\t &= 25\end{aligned}$$

Answer: ..... [2]

13.

The ratio of the number of red marbles to green marbles was 2 : 5. The total number of marbles was 49.

a) How many red marbles were there?

$$\begin{array}{l} \text{Red : green : Total} \\ 2 \quad : \quad 5 \quad : \quad 7 \end{array}$$

$$\begin{aligned}7 \text{ parts} &= 49 \\2 \text{ parts} &= (2 \times 49) / 7 = 14\end{aligned}$$

Answer: ..... [1]

b) When a number of red marbles was added, the new ratio of the red marbles to green marbles was now 8 : 5.

How many red marbles were added?

$$5 \text{ parts} = (5 \times 49) / 7 = 35$$

$$5 \text{ parts} = 35$$

$$8 \text{ parts} = (8 \times 35) / 5 = 56$$

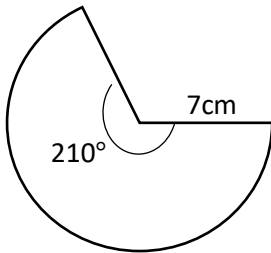
$$\text{Red marbles added} = 56 - 14 = 42$$

Answer: ..... [2]

14.

Calculate the perimeter of a sector of a circle of radius 7cm and angle  $210^\circ$ .

$$\begin{aligned} \text{Perimeter} &= \text{Arc Length} + \text{radius} + \text{radius} \\ &= \frac{210}{360} \times 2 \times \pi \times 7 + 7 + 7 = \\ &39.66 \text{ cm} \\ &= 39.7 \text{ cm (3 s.f.)} \end{aligned}$$



Answer: .....cm [3]

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15.

a) Evaluate  $7^{-3}$ .

$$\begin{aligned} 7^{-3} \\ &= \frac{1}{7^3} \\ &= \frac{1}{343} \end{aligned}$$

Answer: ..... [1]

b) Given that  $8^{\frac{4}{3}} = 2^y$ , find  $y$ .

$$\begin{aligned} 8^{\frac{4}{3}} &= 2^y \\ 2^{3(\frac{4}{3})} &= 2^y \\ 2^4 &= 2^y \\ 4 &= y \\ y &= 4 \end{aligned}$$

Answer: ..... [2]

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16.

The table below shows the weekly number of hours of overtime done by the workers of a company.

No of hours (Overtime)	Number of workers
$0 < x \leq 5$	5
$5 < x \leq 10$	12
$10 < x \leq 15$	40
$15 < x \leq 20$	28
$20 < x \leq 25$	8
$25 < x \leq 30$	7

- a) Find the percentage of employees who did overtime less than or equal to 10 hours per week.

$$17/100 \times 100\% = 17\%$$

Answer: ..... [1]

- b) Find the median.

$$100/2 = 50^{\text{th}} \text{ \& } 51^{\text{st}} \text{ lies in } 10 < x \leq 15$$

$$\text{Median} = 10 < x \leq 15$$

Answer: ..... [1]

- c) Calculate an estimate of the mean number of overtime hours of the workers.

$$\frac{(2.5 \times 5) + (7.5 \times 12) + (12.5 \times 40) + (17.5 \times 28) + (22.5 \times 8) + (27.5 \times 7)}{5 + 12 + 40 + 28 + 8 + 7}$$

Answer: ..... [2]

17.

Factorise

- a)  $2z^2 + z - 10$

	2z	+5
z	2z <sup>2</sup>	5z
-2	-4z	-10

$$2z^2 + z - 10 = (z - 2)(2z + 5)$$

Answer: ..... [2]

- b)  $10ax + 4ay + 15bx + 6by$

$$2a(5x+2y) + 3b(5x+2y)$$

$$= (2a+3b)(5x+2y)$$

Answer: ..... [2]

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18.

- a) A map has a scale of 1 : 200 000. The distance between two cities on the map is 8cm. Calculate the actual distance, in kilometres, between the two cities.

$$\begin{array}{lcl} \text{Map} & : & \text{Actual} \\ 1 & : & 200\,000 \\ 1 & : & 200000/(1000 \times 100) \\ 1 & : & 2\text{km} \\ 8\text{cm} & : & 8 \times 2 = 16\text{km} \end{array}$$

Answer: .....km [2]

- b) A reservoir on the same map covers an area of 14km<sup>2</sup>. Calculate the area, in square centimetres, covered by the reservoir on the map.

$$\begin{array}{lcl} \text{Map} & : & \text{Actual} \\ 1\text{cm} & : & 2\text{km} \\ \text{Area} \Rightarrow (1\text{cm})^2 & : & (2\text{km})^2 \\ 1\text{cm}^2 & : & 4\text{km}^2 \\ 14/4 & : & 14\text{km}^2 \\ 3.5\text{cm}^2 & : & 14\text{km}^2 \end{array}$$

Answer: .....cm<sup>2</sup> [2]

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19.

- a) Solve  $x^2 - x - 6 = 0$

$$\begin{aligned} x^2 - x - 6 &= 0 \\ (x + 2)(x - 3) &= 0 \\ x &= -2 \text{ or } 3 \end{aligned}$$

Answer:  $x = \dots\dots\dots$  or  $\dots\dots\dots$  [2]

- b)  $x^2 - 2x - 6 = (x + a)^2 + b$

By completing the square, determine the values of  $a$  and  $b$ .

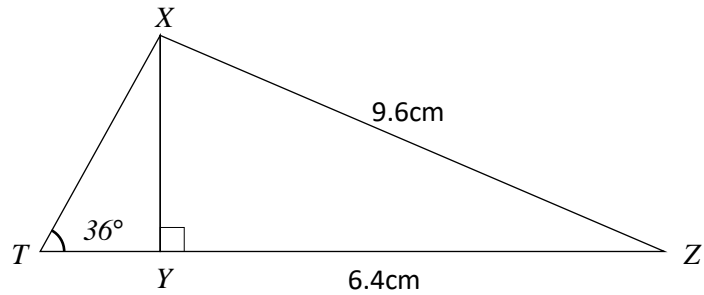
$$\begin{aligned} x^2 - 2x + 1^2 - 6 - 1 \\ (x - 1)^2 - 7 \\ a = -1, b = -7 \end{aligned}$$

Answer:  $a = \dots\dots\dots$  &  $b = \dots\dots\dots$  [2]

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20.

The figure below is made up of two triangles. Triangles TXY and ZXY. In triangle TXY, angle  $\angle XTY = 36^\circ$ . Y is a point on TZ such that XY is perpendicular to TZ.  $YZ = 6.4\text{cm}$  and  $XZ = 9.6\text{cm}$ .



a) Find angle  $\angle YXZ$ .

$$\sin \theta = \frac{6.4}{9.6}$$

$$\theta = \sin^{-1} \frac{6.4}{9.6}$$

$$\theta = 41.8^\circ$$

Answer ..... [2]

b) Find the length of TX.

$$180 - 90 - 41.8 = 48.2$$

$$\frac{\sin 36}{9.6} = \frac{\sin 48.2}{TX}$$

$$TX = \frac{9.6 \times \sin 48.2}{\sin 36}$$

$$TX = 12.2\text{cm}$$

Answer ..... [2]

21.

a) Calculate the gradient of the line joining the points (3,4) and (-1,1).

$$\begin{aligned} m &= \frac{1 - 4}{-1 - 3} \\ &= \frac{-3}{-4} \\ &= \frac{3}{4} \end{aligned}$$

Answer: ..... [2]

bi) Find x given that point (6 , 8) and (x , 11) has the same gradient as (3 , 4) and (-1 , 1)

$$\begin{aligned} \frac{11 - 8}{x - 6} &= \frac{3}{4} \\ \frac{3}{x - 6} &= \frac{3}{4} \\ \frac{12}{3} &= x - 6 \\ 10 &= x \\ \text{Co-ordinates (10,11)} \end{aligned}$$

Answer:  $x =$  ..... [2]

bii) If the line cuts the y-axis at the co-ordinates  $(0, \frac{7}{4})$ , determine the equation of this line.

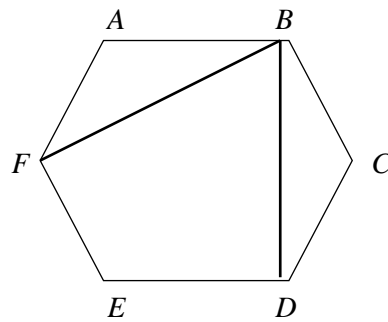
$$\begin{aligned} y &= mx + c \\ y &= 3/4x + c \text{ [Substitute } (0, 7/4)] \\ 7/4 &= 3/4(0) + c \\ c &= 7/4 \\ y &= 3/4x + 7/4 \end{aligned}$$

Answer: ..... [1]

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22.

The figure shows a regular hexagon,  $ABCDEF$ .



a) Find angle  $FBA$ .

$$\frac{(n - 2) \times 180}{n} = \frac{4 \times 180}{6} = 120^\circ$$

$$\text{Angle } FBA = (180 - 120) / 2 = 30^\circ$$

Answer ..... [2]

b) What is a special name given to triangle  $FAB$ .

*triangle  $FAB$  is an isosceles triangle.*

Answer: ..... [1]

c) Find angle  $FBD$ .

$$\text{Angle } ABC = 120^\circ, \text{ angle } FAB \text{ \& } CBD = 30^\circ$$

$$\text{Angle } FBD = 120 - 30 - 30 = 60^\circ.$$

Answer ..... [2]

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23.

Adilah, Adib and Ah Seng wants to buy a computer that costs \$2800.

- a) Adilah paid for the computer in cash was given a discount. Calculate the percentage discount that she received given that she paid \$2380 for the computer.

$$2800 - 2380 = \$420$$
$$420 \div 2800 \times 100\% = 15\%$$

Answer: ..... [2]

- bi) Adib paid an initial deposit of \$400 and paid the rest in monthly instalments of \$150 for a period of 2 years. How much did Adib actually pay for the computer?

$$\text{Adib} = 400 + (150 \times 24) = \$4000$$

Answer: ..... [2]

- bii) Ah Seng decided to take a bank loan to pay for the computer. He has to pay back the loan completely by 2 years. The bank charges a compound interest of 2.5% compounded yearly. Calculate total amount Ah Seng had to pay for the computer.

$$\text{Total} = P(1 + 2.5/100)^2 = \$2941.75$$

Answer: ..... [2]

24.

- a) Find the radius of a sphere that has a surface area of  $255\text{cm}^2$ .

$$4\pi r^2 = 255$$
$$r^2 = 255 \div 4\pi$$
$$r = 4.50$$

Answer: ..... [2]

- b) Find the volume of the same sphere.

$$\text{Vol} = \frac{4}{3} \pi r^3 = 383 \text{ (3 s.f.)}$$

Answer: ..... [2]

- c) The sphere then is melted and formed into a cube. Find the length of a side of the cube.

$$L^3 = 382$$
$$L = 7.26\text{cm (3 s.f.)}$$

Answer: ..... [2]

**Table of Specifications (TOS )**

**Paper 1 Total marks = 80**

<b>Difficulty Level</b>	<b>Simple Question</b>	<b>Sub-Total Marks</b>	<b>Moderate Question</b>	<b>Sub – Total Marks</b>	<b>Challenging Question</b>	<b>Sub-Total Marks</b>
<b>Topic</b>	1, 2, 3, 4, 5, 6, 7, 8, 10	18	12, 13, 14, 15	12	23, 24, 25,26	24
	9, 11	6	18, 19, 20, 21, 22	20		
<b>Total Marks</b>	<b>Simple</b>	<b>24</b>	<b>Moderate</b>	<b>32</b>	<b>Challenging</b>	<b>24</b>
<b>Weightage</b>		<b>30%</b>		<b>40%</b>		<b>30%</b>